

On Computationally-Enhanced Visual Analysis of Heterogeneous Data and Its Application in Biomedical Informatics

Cagatay Turkey¹, Fleur Jeanquartier²
Andreas Holzinger², and Helwig Hauser³

¹ giCentre, Department of Computer Science, City University, London, UK
Cagatay.Turkey.1@city.ac.uk

² Research Unit HCI, Institute for Medical Informatics, Statistics and
Documentation Medical University Graz, Austria
{f.jeanquartier,a.holzinger}@hci4all.at

³ Visualization Group, Department of Informatics, University of Bergen, Norway
Helwig.Hauser@uib.no

Abstract. With the advance of new data acquisition and generation technologies, the biomedical domain is becoming increasingly data-driven. Thus, understanding the information in large and complex data sets has been in the focus of several research fields such as statistics, data mining, machine learning, and visualization. While the first three fields predominantly rely on computational power, visualization relies mainly on human perceptual and cognitive capabilities for extracting information. Data visualization, similar to Human–Computer Interaction, attempts an appropriate interaction between human and data to interactively exploit data sets. Specifically within the analysis of complex data sets, visualization researchers have integrated computational methods to enhance the interactive processes. In this state-of-the-art report, we investigate how such an integration is carried out. We study the related literature with respect to the underlying analytical tasks and methods of integration. In addition, we focus on how such methods are applied to the biomedical domain and present a concise overview within our taxonomy. Finally, we discuss some open problems and future challenges.

Keywords: Visualization, Visual Analytics, Heterogenous Data, Complex Data, Future Challenges, Open Problems.

1 Introduction and Motivation

Our society is becoming increasingly information-driven due to new technologies that provide data at an immense speed and scale. Even scientific practices are going under significant changes to adapt to this tremendous availability of data and data analysis is an important part in answering scientific questions. One of the fields where data analysis is especially important is biomedicine. In this domain, data sets are often structured in terms of both the scales they relate to,

e.g., from molecular interactions to how biological systems in the human body, and the inherent characteristics they carry, e.g., images from different medical devices. Such structures are both a challenge and an opportunity for scientists and significant efforts are put in several domains to understand these data. In this paper, we focus on how visualization, in particular those that incorporate computational analysis, approaches and enhances the analysis of structured information sources. We start with a section that discusses our goals and move on to more specific discussions on understanding information in data.

1.1 Goals

The best way of beginning such a paper, would be to start with the definition of Visualization and discuss the **goal of visualization**: A classical goal of visualization is, in an interactive, visual representation of abstract data, to amplify the acquisition or use of knowledge [1] and to enable humans to gain *insight* into complex data sets, either for the purpose of data exploration and analysis, or for data presentation [2], [3] (see section Glossary and Key Terms for more discussions). Visualization is a form of computing that provides new scientific insight through visual methods and therefore of enormous importance within the entire knowledge discovery process [4].

The **goal of this paper** is to provide a concise introduction into the visualization of large and heterogeneous data sets, in particular from the biomedical domain. For this purpose we provide a glossary to foster a common understanding, give a short nutshell-like overview about the current state-of-the-art and finally focus on open problems and future challenges. We base our taxonomy on a 2D structure on the different analytical tasks and on how computational methods can be integrated in visualizations. All the relevant works are then grouped under these categories. In addition to studies that do not have a specific application domain, we categorize visualization methods that specifically aimed at solving biomedical problems. Such subsets of work are presented under each category.

The **goal of this dual focus strategy** is to identify areas where visualization methods have shown to be successful but have not yet been applied to problems in the biomedical domain.

1.2 Understanding Information in Data

Understanding the relevant information in large and complex data sets has been in the focus of several research fields for quite a time; studies in statistics [5], data mining [6], machine learning [7], and in visualization have devised methods to help analysts in extracting valuable information from a large variety of challenging data sets. While the first three fields predominantly rely on computational power, visualization relies mainly on the perceptual and cognitive capabilities of the human for extracting information. Although these research activities have followed separate paths, there have been significant studies to bring together the strengths from these fields [8–10]. Tukey [11] led the way

in integrating visualization and statistics with his work on **exploratory data analysis**. Earlier research on integrating statistics [12] and data mining [8] with information visualization have taken Tukey's ideas further.

This vision of integrating the best of both worlds has been a highly praised goal in visualization research [13–15] and parallels the emergence of *visual analytics* as a field on its own, which brings together research from visualization, data mining, data management, and human computer interaction [14]. In visual analytics research, the integration of automated and interactive methods is considered to be the main mechanism to foster the construction of knowledge in data analysis. In that respect, Keim [16] describes the details of a visual analysis process, where the data, the visualization, hypotheses, and interactive methods are integrated to extract relevant information. In their sense-making loop, based on the model introduced by van Wijk [17], the analytical process is carried out iteratively where the computational results are investigated through interactive visualizations. Such a loop aims to provide a better understanding of the data that will ultimately help the analyst to build new hypotheses. However, previously presented approaches still lack considering certain research issues to support a truly cross-disciplinary, seamless and holistic approach for the process chain of *data > information > knowledge*. Research needs to deal with data integration, fusion, preprocessing and data mapping as well as issues of privacy and data protection. These issues are being addressed in the HCI-KDD approach by Holzinger [18], [19] and is supported by the international expert network HCI-KDD (see hci4all.at).

1.3 Understanding Information in Biomedical Data

Interactive visual methods have been utilized within a wide spectrum of domains. In biomedicine, visualization is specifically required to support data analysts in tackling with problems inherent in this domain [19–21]. These can be summarized in three specific and general challenges:

Challenge 1: Due to the trend towards a data-centric medicine, data analysts have to deal with increasingly growing volumes and a diversity of highly complex, multi-dimensional and often weakly-structured and noisy data sets and increasing amounts of unstructured information.

Challenge 2: Due to the increasing trend towards precision medicine (P4 medicine: Predictive, Preventive, Participatory, Personalized (Hood and Friend, 2011)), biomedical data analysts have to deal with results from various sources in different structural dimensions, ranging from the microscopic world (systems biology, see below), and in particular from the "Omics-world" (data from genomics, proteomics, metabolomics, lipidomics, transcriptomics, epigenetics, microbiomics, fluxomics, phenomics, etc.) to the macroscopic world (e.g., disease spreading data of populations in public health informatics).

Challenge 3: The growing need for *integrative* solutions for interactive visualization of the data mentioned in challenge 1 and 2. Note that, although there are many sophisticated results and paradigms from the visualization community, integrated solutions, e.g. within business hospital information systems, are rare today.

An example from the biological domain can emphasize the aforementioned challenges: Biologists deal with data of different scale and resolution, ranging from tissues at the molecular and cellular scale ("the microscopic") up to organ scale ("the macroscopic"), as well as data from a diversity of databases of genomes and expression profiles, protein-protein interaction and pathways [22]. As understood by *systems biology*, the biological parts do not act alone, but in a strongly interwoven fashion, therefore biologists need to bridge and map different data types and analyze interactions [23]. Biomedicine has reached a point where the task of analyzing data is replacing the task of generating data [24]. At this point, visual analysis methods that support knowledge discovery in complex data become extremely important.

2 Glossary and Key Terms

In this section, we try to capture visualization and data analysis related terms that are only referenced explicitly within this paper. We do not cover the whole spectrum of visualization and analysis terms.

Visualization: is a visual representation of data sets intended to help people carry out some task more effectively according to Tamara Munzner [25]. Ward describes visualization as the graphical presentation of information, with the goal of providing the viewer with a qualitative understanding of the information contents [3].

Space: A set of points $a \in \mathbb{S}$ which satisfy some geometric postulate.

Topological Visualization: a prominent trend in current visualization research, driven by the data deluge. A topological abstraction provides a common mathematical language to identify structures and contexts [26], [27].

Visual Analytics: is an integrated approach combining visualization, human factors and data analysis to achieve a deep understanding of the data [13, 14].

Interactive Visual Analysis (IVA): is a set of methods that have overlaps with visual analytics. It combines the computational power of computers with the perceptive and cognitive capabilities of humans to extract knowledge from large and complex data sets. These techniques involve looking at data sets through different, linked views and iteratively selecting and examining features the user finds interesting.

Heterogeneous Data: composed of data objects carrying different characteristics and coming from different sources. The heterogeneity can manifest itself in several forms such as different *scales of measure*, i.e., being categorical, discrete or continuous, or challenging to relate representations, e.g., genomic activity through gene expression vs. molecular pathways; a recent example of such data sets is described by Emmert-Streib et al. [28].

Classification: Methods that identify which subpopulation a new observation belongs on the basis of a training set of observations with known categories.

Factor Analysis and Dimension Reduction: is a statistical method that aims to describe the information in the data by preserving most of the variety. This process often leads to derived, unobserved variables called the factors [5]. Similarly, there exist dimension reduction methods, such as Principal Component Analysis (PCA) and Multi-Dimensional Scaling (MDS) that project higher dimensional data onto lower dimensional spaces by preserving the variance in the data [5].

Decision Tree: is a predictive statical model that enhances classification tasks [29]. It is often represented visually as a tree to support decision making tasks (see Figure 4).

Regression Analysis: is a statistical method that aims to estimate the relations between data variables. In other words, it tries to model how dependent certain factors are on others in the data [30].

3 State of the Art

There are a number of surveys that characterize how the integration of automated methods and interactive visualizations are accomplished. Crouser and Chang [31] characterize the human computer collaboration by identifying what contributions are made to the process by the two sides. In their survey, several papers are grouped according to these types of contributions. According to the authors, humans contribute to the analytical processes mainly by *visual perception, visuospatial thinking, creativity and domain knowledge*. On the other side, the computer contributes by *data manipulation, collection and storing, and bias-free analysis routines*. Bertini and Lalanne [15] categorize methods involving data mining and visualization into three: *computationally enhanced visualization, visually enhanced mining, and integrated visualization and mining*. Their categorization depends on whether it is the visualization or the automated method that plays the major role in the analysis.

In this state of the art analysis, we categorize the related literature in two perspectives. Our first perspective relates to the analytical task that is being carried out. After an investigation of literature from the computational data analysis domain [5, 32, 33], we identify a general categorization of the most common data analysis tasks as follows: *summarizing information, finding groups &*

classification, and *investigating relations & prediction*. We discuss these tasks briefly under each subsection in the following. Our second perspective relates to how the integration of computational tools in visual analysis is achieved. We identify three different categories to characterize the level of integration of computational tools in visualization, namely, *visualization as a presentation medium*, *semi-interactive use of computational methods* and the *tight integration of interactive visual and computational tools*. These levels are discussed in detail in Section 3.1.

In the following, we firstly organize the literature under the three analytical task categories and then group the related works further in sub-categories relating to the levels of integration. Before we move on to the literature review, we describe the three levels of integration introduced above. Even though we describe each analysis task separately, the categorization into the three common analysis tasks can be seen as a series of steps within a single analysis flow. Starting with summarizing information, proceeding with finding groups and last but not least finding relations and trends. One aspect that we do not cover explicitly is the consideration of outliers. Outlier analysis focuses on finding elements that do not follow the common properties of the data and needs to be part of a comprehensive data analysis process [34]. In this paper, we consider outlier analysis as an inherent part of summarizing information although there are works that are targeted at treating outliers explicitly [35].

Table 1 groups the investigated literature under the categories listed here. One important point to make with respect to the allocations to sub-groups in this table is that the borders within the categories are not always clear and there is rather a smooth transition between the categories. There are methods that try to address more than one analytical question. For such works, we try to identify the core questions tackled to place them in the right locations in this table. Similar smooth transitions also exist for the levels of integration, and our decision criteria is discussed in the following section.

3.1 Levels of Integration

On the first level of integration of computational tools within visual data analysis, visualization is used as a presentation medium to communicate the results of computational tools. These visualizations are either static representations, or only allow limited interaction possibilities such as zooming, panning, or making selections to highlight interesting parts of the data. A typical example for this category is the use of graphical plotting capabilities of statistical analysis software such as R [36]. In this system, users often refer to static visualizations to observe the results from computational procedures, such as clustering or fitting a regression line.

The second level of integration involves the use of the computational tool as a separate entity within the analysis where the tool's inner working is not transparent to the user. In this setting, the user interacts with the computational mechanism either through *modifying parameters* or *altering the data domain* being analyzed. The results are then presented to the user through different

Table 1. Analytical Tasks vs. Levels of Integration. This 2D structure is used to categorize the reviewed literature in this paper.

	Visualization as presentation	Semi-interactive Methods	Tight Integration
Summarizing Information	[37], [24]	[38], [39], [40], [41], [42], [43], [44], [45], [46], [47], [48], [49] [50]	[51], [52], [53], [54], [55], [56]
Groups & Classification	[57] [58], [59]	[60], [61], [62], [63], [64], [65], [66], [67], [68], [69], [70], [71], [72], [73], [74]	[75], [76], [77], [78], [79], [80]
Dependence & Prediction	[81], [82], [46]	[83], [84], [85], [86], [87], [88], [89]	[90], [91], [92]

visual encodings that are often accompanied by interaction. One potential benefit here is that if problems are just too large so that a comprehensive computational approach is totally unfeasible, for ex., exhaustively searching a high-dimensional parameter space, then some directed steering by the intelligent expert user can help.

The third level constitutes mechanisms where a tight integration of interactive methods and computational tools is achieved. In these approaches, the automated methods are used seamlessly within interactive visual analysis. Sophisticated interaction mechanisms make the automated tools an integral part of the visualization. Methods in this category also interfere with the inner working of the algorithms and the results of automated tools are communicated immediately to the user.

When the second and the third levels are considered, we observe that categorizing a paper is not straightforward since the boundaries between these levels are smooth rather than discrete. In that respect, our classification criteria for level three is whether the integration allows for flexibility and done in a seamless way. If the integration is done at a manner where the automated method exists explicitly as a black-box that allows interaction to a certain level, we categorize the method under level two.

3.2 Summarizing Information

Data sets are becoming large and complex both in terms of the number of items and the number of modalities, i.e., data measured/collected from several sources, they contain. In order to tackle with the related visualization challenges, methods that are based on the summarization of underlying information are widely used in both automated and interactive visual data analysis [93]. Methods in this category involve the integration of descriptive statistics, dimension reduction, and factor analysis methods in general.

Visualization as Presentation

For this category, we focus only on visualization tools in the biomedical context where there are many examples for visualization as presentation. As databases have become an integral part of dissemination and mining in biomedicine, the consolidation of such experiments data already brought up comprehensive tools for managing and sharing data. To name one, the Cell Centered Database [37] is a public image repository for managing and sharing (3D) imaging data. Next to image databases there is also a wide variety of different visualization tools, including interaction networks, pathway visualizations, multivariate omics data visualizations and multiple sequence alignments that have been reviewed recently by others [23, 24, 94]. In this context, visualization is most commonly used for exploration (hypothesis generation). Common visualization methods in addition to network visualization include scatter plots, profile plots/parallel coordinates and heatmaps with dendrograms, while many tools provide combinations of those as linked views. Comprehensive summaries of visualization tools exist for certain areas. Nielsen et al. [24] present a review on tools for visualizing genomes, in particular tools for visualizing sequencing data, genome browsers and comparative genomics. Gehlenborg et al. [23] present a table of visualization tools in the area of systems biology, categorized by the different focusses of omics data. While most tools still lack in usability and integration, some of the listed tools already provide sophisticated interactive possibilities like annotating, comparing and showing confidence measures and prediction results next to view manipulations such as navigating, zooming and filtering. There is also a trend towards implementing web-based solutions to facilitate collaboration.

Semi-interactive Methods

Perer and Shneiderman [45] discuss the importance of combining computational analysis methods, in particular statistics, with visualization to improve exploratory data analysis. Jänicke et al. [38] utilize a two-dimensional projection method (see Figure 1) where the analysis is performed on a projected 2D space called the attribute cloud. The resulting point cloud is then used as the medium for interaction where the user is able to brush and link the selections to other views of the data. Johansson and Johansson [39] enable the user to interactively reduce the dimensionality of a data set with the help of quality metrics. The visually guided variable ordering and filtering reduces the complexity of the data in a transparent manner where the user has a control over the whole process. The authors later use this methodology in the analysis of high-dimensional data sets involving microbial populations [40]. Fuchs et al. [41] integrate methods from machine learning with interactive visual analysis to assist the user in knowledge discovery. Performing the high-dimensional data analysis on derived attributes is a strategy utilized in a number of studies. Kehrer et al. [49] integrate statistical moments and aggregates to interactively analyze collections of multivariate data sets. In the VAR display by Yang et al. [48], the authors

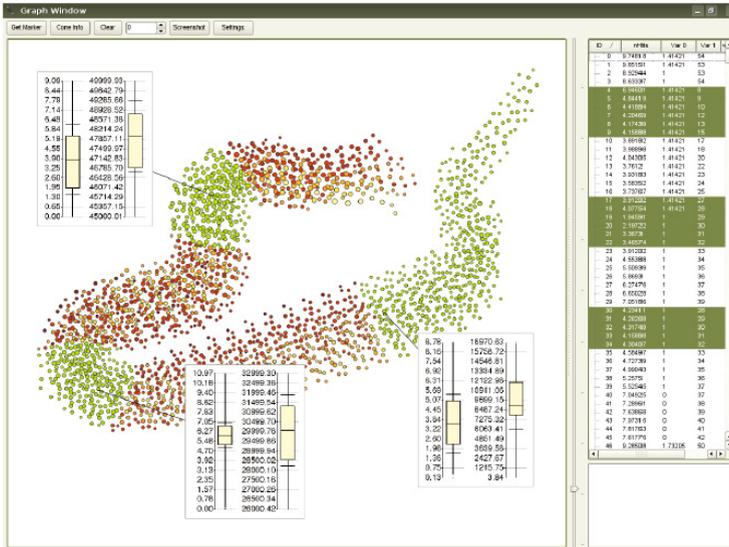


Fig. 1. Data can be visually analyzed on interactively created 2D spaces. (Image by Jänicke et al. [38]).

represent the dimensions as glyphs on a 2D projection of the dimensions. A multidimensional scaling operation is performed on the glyphs where the distances between the dimensions are optimally preserved in the projection.

In Biomedicine there are only a few visualization tools that are being used to construct integrated web applications for interactive data analysis. Next to the UCSC Genome Browser [46], the IGV [47] is another common genome browser that integrates many different and large data sets and supports a wide variety of data types to be explored interactively. A few similar tools that are tightly integrated with public databases for systems biology are listed by Gehlenborg et al. [23].

In MulteeSum, Meyer et al. [50] used visual summaries to investigate the relations between linked multiple data sets relating to gene expression data. Artemis [43] supports the annotation and visual inspection, comparison and analysis of high-throughput sequencing experimental data sets. The String-DB [44] is a commonly used public comprehensive database for protein-protein interaction that supports visual data analysis by providing interactive network visualizations.

Otasek et al. [95] present a work on Visual Data Mining (VDM), which is supported by interactive and scalable network visualization and analysis. Otasek et al. emphasize that knowledge discovery within complex data sets involves many workflows, including accurately representing many formats of source data, merging heterogeneous and distributed data sources, complex database searching,

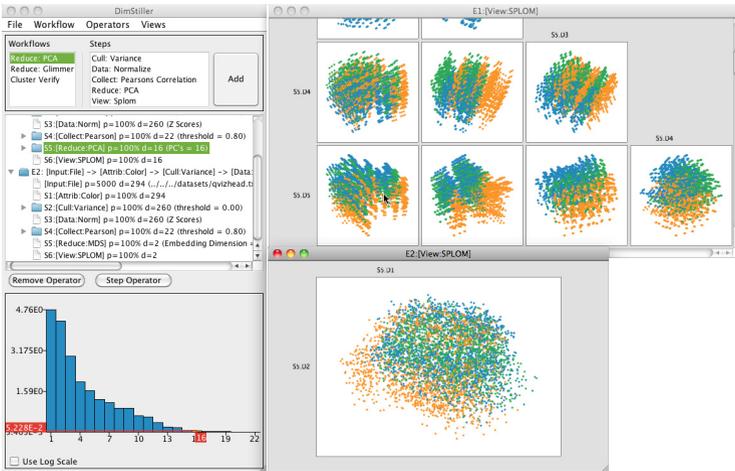


Fig. 2. A selection of data transformations are chained together interactively to achieve dimension reduction. (Image by Ingram et al. [54]).

integrating results from multiple computational and mathematical analyses, and effectively visualizing properties and results.

Mueller et al. report in a recent work [96] on the successful application of data Glyphs in a disease analyser for the analysis of big medical data sets with automatic validation of the data mapping, selection of subgroups within histograms and a visual comparison of the value distributions.

Tight Integration

Nam and Mueller [51] provides the user with an interface where a high-dimensional projection method can be steered according to user input. In MDSteer [52], an embedding is guided with user interaction leading to an adapted multidimensional scaling of multivariate data sets. Such a mechanism enables the analyst to steer the computational resources accordingly to areas where more precision is needed. Ingram et al. [54] present a system called DimStiller, where a selection of data transformations are chained together interactively to achieve dimension reduction (see Figure 2). Endert et al. [53] introduce observation level interactions to assist computational analysis tools to deliver more reliable results. The authors describe such operations as enabling the *direct manipulation* for visual analytics [55]. Turkey et al. introduce the dual-analysis approach [56] to support analysis processes where computational methods such as dimension reduction [92] are used.

3.3 Finding Groups and Classification

One of the most common analytical tasks in data analysis is to determine the different groups and classifications [5]. Analysts often employ cluster analysis methods that divide data into clusters where data items are assigned to groups that are similar with respect to certain criteria [97]. One aspect of cluster analysis is that it is an unsupervised method, i.e., the number of groups or their labels are not known a priori. However, when the analyst has information on class labels beforehand, often referred to as *the training set*, classification algorithms can be utilized instead. Below, we list interactive visualization methods where cluster analysis tools and/or classification algorithms are utilized.

Visualization as Presentation

Parallel Sets by Kosara et al. [58] is a successful example where the overlaps between groups is presented with a limited amount of interaction. In the software visualization domain, Telea and Auber [59] represent the changes in code structures using a flow layout where they identify steady code blocks and when splits occur in the code of a software. Demvsar et al. [57] present a visualization approach for exploratory data analysis of multidimensional data sets and show its utility for classification on several biomedical data sets.

Semi-interactive Methods

May and Kohlhammer [64] present a conceptual framework that improves the classification of data using decision trees in an interactive manner. The authors later proposed a technique called SmartStripes [65] where they investigate the relations between different subsets of features and entities. Interactive systems have also been used to help create decision trees [98] (see Figure 4). Guo et al. [70] enable the interactive exploration of multivariate model parameters. They visualize the model space together with the data to reveal the trends in the data. Kandogan [71] discusses how clusters can be found and annotated through an image-based technique. Rinzivillo et al. [72] use a visual technique called progressive clustering where the clustering is done using different distance functions in consecutive steps. Schreck et al. [73] propose a framework to interactively monitor and control Kohonen maps to cluster trajectory data. The authors state the importance of integrating the expert within the clustering process in achieving good results. gCluto [74] is an interactive clustering and visualization system where the authors incorporate a wide range of clustering algorithms.

In *Hierarchical Clustering Explorer* [69], Seo and Shneiderman describe the use of an interactive dendrogram coupled with a colored heatmap to represent clustering information within a coordinated multiple view system. Other examples include works accomplished within the Caleydo software for pathway analysis and associated experimental data by Lex et al. [60–62]. In a recent work (see Figure 3), the integrated use of statistical computations is shown to

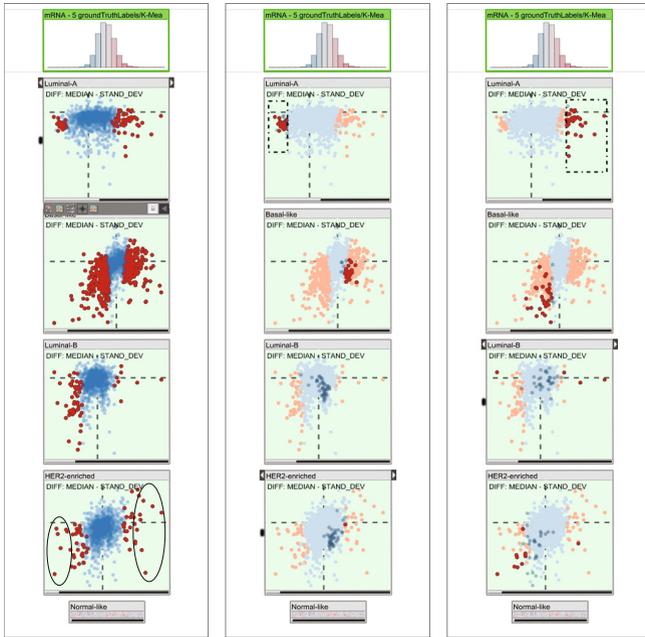


Fig. 3. Results of statistical test computations are communicated through visual encodings to support the identification of discriminative elements in subgroups. (Image by Turkay et al. [63]).

be useful to characterize the groupings in the data [63]. Gehlenborg et al. [23] identified that scatter plots, profile plots and heat maps are the most common visualization techniques used in interactive visualization tools for tasks like gene expression analysis. Younesy et al. [66] presents a framework where users have the ability to steer clustering algorithms and visually compare the results. Dynamically evolving clusters, in the domain of molecular dynamics, are analyzed through interactive visual tools by Grottel et al. [67]. The authors describe flow groups and a schematic view that display cluster evolution over time. Mayday is one framework example where a visual analytics framework supports clustering of gene expression data sets [68].

Tight Integration

Turkay et al. presents an interactive system that addresses both the generation and evaluation stages in a clustering process [79]. Another example is the iVisClassifier by Choo et al. [80] where the authors improve classification performance through interactive visualizations. Ahmed and Weaver [75] discuss how the clustering process can be embedded within an highly interactive system. Examples in biomedical domain are rare in this category. One example is by Rubel

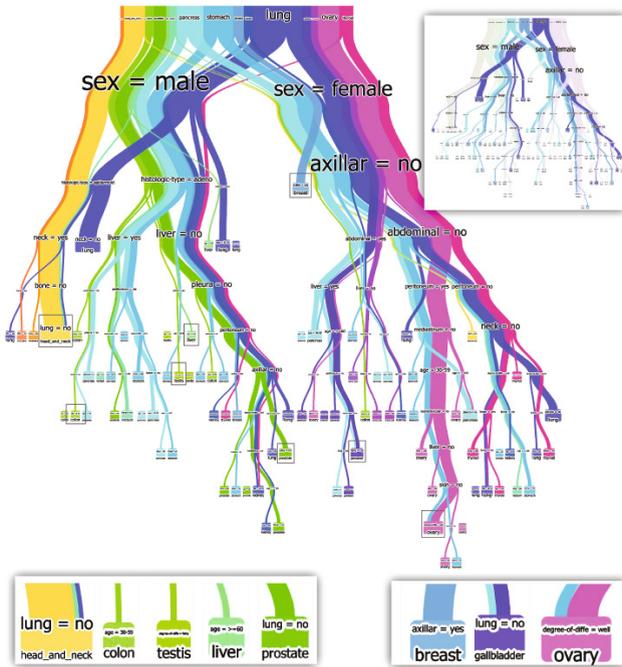


Fig. 4. Interactive systems have been used to help create and evaluate decision trees (Image by van den Elzen and van Wijk [98])

et al. [76], who present a framework for clustering and visually exploring (3D) expression data. In the domain of molecular dynamics simulation, there are some examples of tight integrations of interactive visualizations, clustering algorithms, and statistics to support the validity of the resulting structures [77], [78].

3.4 Investigating Dependence

An often performed task in data analysis is the investigation of relations within different features in a data set [99]. This task is important to build cause and effect relations, understanding the level of dependence between features, and predicting the possible outcomes based on available information. In this category, we list interactive methods that incorporate computational tools to facilitate such tasks. Often employed mechanisms are: regression, correlation, and predictive analysis approaches. In the biomedical domain, Serrier et al. [100] present a list of tools that deal with the issue of time, however, they note that it is yet an open challenge in comparative genomics to find tools for analyzing time series data that can handle both the visualization of changes as well as showing trends and predictions for insightful inferences and correlations.



Fig. 5. Visualization helps analysts in making predictions and investigating uncertainties in relations within simulation parameters (Image by Booshehrian et al. [86])

3.5 Visualization as Presentation

In this category, we focus mainly on works from biomedical domain. Krzywinski et al. [81] presents a tool for comparative genomics by visualizing variation in genome structure. Karr et al. [82] present a promising topic, namely computing comprehensive whole-cell model and presenting model predictions for cellular and molecular properties.

Nielsen et al. [24] reviews tools for the visual comparison of genomes. The list of referenced tools includes Circos [81], a visualization presentation method for visualizing synteny (genetic linkage) in a circular layout. One example referenced is the already mentioned UCSC genome browser [46] that also provides simple phylogenetic tree graphs. The list also includes tools that integrate computational methods and support the visual analysis of comparative genomics more interactively, which are discussed in the next level of integration.

3.6 Semi Interactive Visualization

Visualization has shown to be effective in validating predictive models through interactive means [84]. Mühlbacher and Piringer [85] (see Figure 6) discuss how the process of building regression models can benefit from integrating domain knowledge. In the framework called Vismon, visualization has helped analysts to make predictions and investigate the uncertainties that are existent in relations within simulation parameters [86] (see Figure 5). Interaction methods facilitate the investigation of multivariate relations in multi-variate data sets [88]. Yang

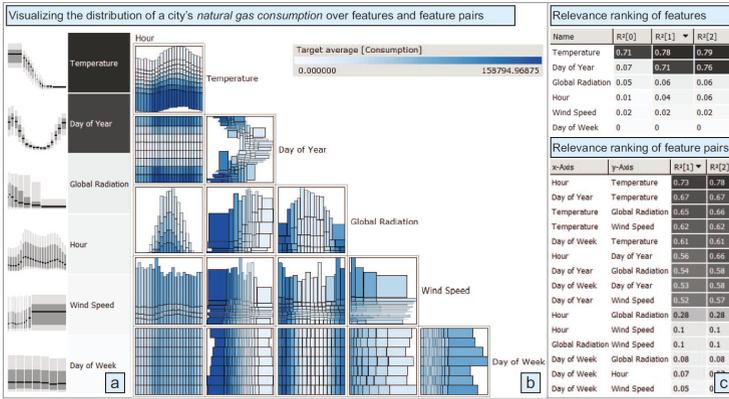


Fig. 6. The process of building regression models can benefit from integrating domain knowledge through interactive visualizations. (Image by Mühlbacher and Piringer [85]).

et al. [89] analyze the relations between the dimensions of a data set to create a hierarchy that they later use to create lower-dimensional spaces.

Within biomedical applications, Meyer et al. [83] present a synteny browser called MizBee, that provides circular views for the interactive exploration and analysis of conserved synteny relationships at multiple scales. In a later paper, they investigate the dependencies within signals coming from related data sets and present a comparative framework [87].

3.7 Tight Integration

Berger et al. [90] introduce an interactive approach that enables the investigation of the parameter space with respect to multiple target values. Malik et al. [91] describe a framework for interactive auto-correlation. This is an example where the correlation analysis is tightly coupled with the interactive elements in the visualization solution. Correlation analysis have been integrated as an internal mechanism to investigate how well lower-dimensional projections relate to the data that they represent [92].

4 Open Problems

Nearly 10 years ago, Chaomei Chen (2005) [101] raised a list of top 10 unsolved information visualization problems, interestingly on top are usability issues, which are particularly relevant for the biomedical domain, and still unsolved today, as a recent study has shown [102]. This is mostly due to the fact that usability engineering methods are still considered as nice add-on and not yet an integrated part in the software development process [103]. Here we list a number of open problems in relation to the literature we cover in this report.

Problem 1. A topic that needs further attention is to address the uncertainty within the analysis process. The explorative nature of interactive visual analysis creates a vast amount of analysis possibilities and often leads to several plausible results. It is thus of great importance to reduce this space of possibilities and inform the user about the certainty of the results.

Problem 2. Although we have seen several works that involve a tight integration between computational methods and visualization, examples of *seamless integrations* are rare. With this term, we refer to interaction mechanisms where the support from appropriate sophisticated computational tools are provided to the user without the analyst noticing the complexities of the underlying mechanisms. One example to clarify this term could be: applying regression analysis locally on a selection within a 2D scatterplot and presenting the result immediately with a regression line.

Problem 3. One aspect that needs to be investigated further in the integration of interactive and automated methods is the *issue of usability*. Most of the solutions introduced here require significant literacy in statistics and skills in using different computational methods – which can lead to a demanding learning curve.

Problem 4. We have seen that most of the visual analysis methods are focussed at particular data types. However, given the current state of data collection and data recording facilities, there are often several data sets related to a phenomenon. There is the need for advanced mechanisms that can harness these various sources of information and help experts to run analysis that stretches over several data sets. This issue relates to the goal of developing an integrated visualization environment spanning several biological dimensions, from micro to macro towards an integrated approach. The recent survey by Kehrer and Hauser [104], which illustrates the many different axes along which data complexity evolves and how visualization can address these complexities, is a starting point to identify suitable approaches.

Problem 5. One observation we make is that the visualization methods often use the support from a single, specific computational mechanism. However, in order to achieve a comprehensive data analysis session, one needs to address all of the analysis tasks we present in our discussions above from summarizing information up to finding cause and effect [22, 100]. Especially, when works relating to biomedical applications are considered, we notice that studies that involve the tight integration of computational tools are rare. Given the successful application of such methods in other domains, it is expected that biomedical applications can also benefit significantly from these approaches.

5 Future Outlook

As stated within the open problems above, there is a certain need for mechanisms to improve the interpretability and usability of interactive visual analysis

techniques. Possible methods could be to employ *smart labeling and annotation*, creating *templates that analysts can follow* for easier progress, and *computationally guided interaction* mechanisms where automated methods are *integrated seamlessly*. Such methods need to utilize computational tools as underlying support mechanism for users, one aspect that needs attention in this respect is to maintain the interactivity of the systems. Appropriate computation and sampling mechanisms needs to be developed to achieve such systems.

In order to address the uncertainties in visual data analysis, mechanisms that communicate the reliability of the observations made through interactive visualizations need to be developed, e.g., what happens to the observation if the selection is moved slightly along the x-axis of a scatter plot? If such questions are addressed, interactive and visual methods could easily place themselves in the everyday routine of analysts that require precise results.

The ability to define features interactively and refine feature definitions based on insights gained during visual exploration and analysis provides an extremely powerful and versatile tool for knowledge discovery. Future challenges lie in the integration of alternate feature detection methods and their utilization in intelligent brushes. Furthermore, integrating IVA and simulations, thus supporting computational steering, offers a wide range of new possibilities for knowledge discovery [105].

An interesting direction for future research relates to improving the usability of analysis processes. Current usability studies often focus on specific parts of a technique. However in order to evaluate the effectiveness of the whole analysis process, there is the need to perform comprehensive investigations on the interpretability of each step of the analysis and study the effects of using computational tools interactively. Such studies can be carried out in forms of controlled experiments where the analysts are given well-determined tasks and are asked to employ particular types of analysis routes. These routes can then be evaluated and compared against non-interactive processes where possible.

A challenging future research avenue for effective HCI is to find answers to the question “What is interesting?” as *Interest* is an essentially human construct [106], a perspective on relationships between data that is influenced by context, tasks, personal preferences, previous knowledge (=expectations) and past experience [107]. For a correct semantic interpretation, a computer would need to understand the *context* in which a visualization is presented; however, comprehension of a complex context is still beyond computation. In order for a data mining system to be generically useful, it must therefore have some way in which one can indicate what is interesting, and for that to be dynamic and changeable [108].

A recent research route in HCI is *Attention Routing*, which is a novel idea introduced by Polo Chau [109] and goes back to models of attentional mechanisms for forming position-invariant and scale-invariant representations of objects in the visual world [110]. Attention routing is a promising approach to overcome one very critical problem in visual analytics, particularly of large and heterogeneous data sets: to help users locate good starting points for their analysis. Based

on *anomaly detection* [111], attention routing methods channel the end-users to interesting data subsets which do not conform to standard behaviour. This is a very promising and important research direction for Knowledge Discovery and Data Mining [18].

Top end research routes encompassing uncountable research challenges are in the application of computational topology [26], [112], [113] approaches for data visualization. Topology-based methods for visualization and visual analysis of data are becoming increasingly popular, having their major advantages in the capability to provide a concise description of the overall *structure* of a scientific data set, because subtle features can easily be missed when using traditional visualization methods (e.g. volume rendering or isocontouring), unless correct transfer functions and isovalues are chosen. By visualizing a topology directly, one can guarantee that no feature is missed and most of all solid mathematical principles can be applied to simplify a topological structure. The topology of functions is also often used for feature detection and segmentation (e.g., in surface segmentation based on curvature) [114].

In this state-of-the-art report, we investigated the literature on how visualization and computation support each other to help analysts in understanding complex, heterogeneous data sets. We also focused on to what degree these methods have been applied to biomedical domain. When the three different levels of integration are considered, we have observed that there are not yet many works falling under the third integration level. We have seen that existing applications in this category have significant potential to address the challenges discussed earlier in the paper. However, there exist several open problems, which can motivate the visualization and knowledge discovery community to carry out research on achieving a tight integration of computational power and capabilities of human experts.

References

1. Card, S.K., Mackinlay, J.D., Shneiderman, B.: Information Visualization: Using Vision to Think. Morgan Kaufmann, San Francisco (1999)
2. Moeller, T., Hamann, B., Russell, R.D.: Mathematical foundations of scientific visualization, computer graphics, and massive data exploration. Springer (2009)
3. Ward, M., Grinstein, G., Keim, D.: Interactive data visualization: Foundations, techniques, and applications. AK Peters, Ltd. (2010)
4. Holzinger, A., Dehmer, M., Jurisica, I.: Knowledge discovery and interactive data mining in bioinformatics - state-of-the-art, future challenges and research directions. BMC Bioinformatics 15(suppl. 6), I1 (2014)
5. Johnson, R., Wichern, D.: Applied multivariate statistical analysis, vol. 6. Prentice Hall, Upper Saddle River (2007)
6. Tan, P.N., Steinbach, M., Kumar, V.: Introduction to Data Mining. Addison-Wesley Longman Publishing Co., Inc. (2005)
7. Alpaydin, E.: Introduction to machine learning. MIT press (2004)
8. Keim, D.: Information visualization and visual data mining. IEEE Transactions on Visualization and Computer Graphics 8(1), 1–8 (2002)

9. Shneiderman, B.: Inventing discovery tools: Combining information visualization with data mining. *Information Visualization* 1(1), 5–12 (2002)
10. Ma, K.L.: Machine learning to boost the next generation of visualization technology. *IEEE Computer Graphics and Applications* 27(5), 6–9 (2007)
11. Tukey, J.W.: *Exploratory Data Analysis*. Addison-Wesley (1977)
12. Cleveland, W.S., Mac Gill, M.E.: *Dynamic graphics for statistics*. CRC Press (1988)
13. Thomas, J.J., Cook, K.A.: *Illuminating the Path: The Research and Development Agenda for Visual Analytics*. National Visualization and Analytics Ctr (2005)
14. Keim, D.A., Kohlhammer, J., Ellis, G., Mansmann, F.: *Mastering The Information Age-Solving Problems with Visual Analytics*. Florian Mansmann (2010)
15. Bertini, E., Lalanne, D.: Investigating and reflecting on the integration of automatic data analysis and visualization in knowledge discovery. *SIGKDD Explor. Newsl.* 11(2), 9–18 (2010)
16. Keim, D.A., Andrienko, G., Fekete, J.-D., Görg, C., Kohlhammer, J., Melançon, G.: Visual analytics: Definition, process, and challenges. In: Kerren, A., Stasko, J.T., Fekete, J.-D., North, C. (eds.) *Information Visualization*. LNCS, vol. 4950, pp. 154–175. Springer, Heidelberg (2008)
17. van Wijk, J.J.: The value of visualization. In: *IEEE Visualization, VIS 2005*, pp. 79–86. IEEE (2005)
18. Holzinger, A.: Human-computer interaction and knowledge discovery (hci-kdd): What is the benefit of bringing those two fields to work together? In: Cuzzocrea, A., Kittl, C., Simos, D.E., Weippl, E., Xu, L. (eds.) *CD-ARES 2013*. LNCS, vol. 8127, pp. 319–328. Springer, Heidelberg (2013)
19. Holzinger, A., Jurisica, I.: Knowledge discovery and data mining in biomedical informatics: The future is in integrative, interactive machine learning solutions. In: Holzinger, A., Jurisica, I. (eds.) *Interactive Knowledge Discovery and Data Mining in Biomedical Informatics: State-of-the-Art and Future Challenges*. LNCS, vol. 8401, pp. 1–17. Springer, Heidelberg (2014)
20. Holzinger, A.: On knowledge discovery and interactive intelligent visualization of biomedical data - challenges in humancomputer interaction and biomedical informatics. In: *DATA 2012*, pp. 9–20. INSTICC (2012)
21. Fernald, G.H., Capriotti, E., Daneshjou, R., Karczewski, K.J., Altman, R.B.: Bioinformatics challenges for personalized medicine. *Bioinformatics* 27(13), 1741–1748 (2011)
22. O’Donoghue, S.I., Gavin, A.C., Gehlenborg, N., Goodsell, D.S., Hériché, J.K., Nielsen, C.B., North, C., Olson, A.J., Procter, J.B., Shattuck, D.W., et al.: Visualizing biological data now and in the future. *Nature Methods* 7, S2–S4 (2010)
23. Gehlenborg, N., O’Donoghue, S., Baliga, N., Goesmann, A., Hibbs, M., Kitano, H., Kohlbacher, O., Neuweger, H., Schneider, R., Tenenbaum, D., et al.: Visualization of omics data for systems biology. *Nature Methods* 7, S56–S68 (2010)
24. Nielsen, C.B., Cantor, M., Dubchak, I., Gordon, D., Wang, T.: Visualizing genomes: techniques and challenges. *Nature Methods* 7, S5–S15 (2010)
25. Munzner, T.: Visualization principles. Presented at VIZBI 2011: Workshop on Visualizing Biological Data (2011)
26. Hauser, H., Hagen, H., Theisel, H.: *Topology-based methods in visualization (Mathematics+Visualization)*. Springer, Heidelberg (2007)
27. Pascucci, V., Tricoche, X., Hagen, H., Tierny, J.: *Topological Methods in Data Analysis and Visualization: Theory, Algorithms, and Applications (Mathematics+Visualization)*. Springer, Heidelberg (2011)

28. Emmert-Streib, F., de Matos Simoes, R., Glazko, G., McDade, S., Haibe-Kains, B., Holzinger, A., Dehmer, M., Campbell, F.: Functional and genetic analysis of the colon cancer network. *BMC Bioinformatics* 15(suppl. 6), S6 (2014)
29. Olshen, L.B.J.F.R., Stone, C.J.: Classification and regression trees. Wadsworth International Group (1984)
30. Cohen, J., Cohen, P., West, S.G., Aiken, L.S.: Applied multiple regression/correlation analysis for the behavioral sciences. Lawrence Erlbaum (2003)
31. Crouser, R.J., Chang, R.: An affordance-based framework for human computation and human-computer collaboration. *IEEE Transactions on Visualization and Computer Graphics* 18(12), 2859–2868 (2012)
32. Brehmer, M., Munzner, T.: A multi-level typology of abstract visualization tasks. *IEEE Transactions on Visualization and Computer Graphics* 19(12), 2376–2385 (2013)
33. Kerren, A., Ebert, A., Meyer, J. (eds.): GI-Dagstuhl Research Seminar 2007. LNCS, vol. 4417. Springer, Heidelberg (2007)
34. Filzmoser, P., Hron, K., Reimann, C.: Principal component analysis for compositional data with outliers. *Environmetrics* 20(6), 621–632 (2009)
35. Novotný, M., Hauser, H.: Outlier-preserving focus+context visualization in parallel coordinates. *IEEE Transactions on Visualization and Computer Graphics* 12(5), 893–900 (2006)
36. R Core Team: R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Vienna, Austria (2013)
37. Martone, M.E., Tran, J., Wong, W.W., Sargis, J., Fong, L., Larson, S., Lamont, S.P., Gupta, A., Ellisman, M.H.: The cell centered database project: An update on building community resources for managing and sharing 3d imaging data. *Journal of Structural Biology* 161(3), 220–231 (2008)
38. Jänicke, H., Böttinger, M., Scheuermann, G.: Brushing of attribute clouds for the visualization of multivariate data. *IEEE Transactions on Visualization and Computer Graphics*, 1459–1466 (2008)
39. Johansson, S., Johansson, J.: Interactive dimensionality reduction through user-defined combinations of quality metrics. *IEEE Transactions on Visualization and Computer Graphics* 15(6), 993–1000 (2009)
40. Fernstad, S., Johansson, J., Adams, S., Shaw, J., Taylor, D.: Visual exploration of microbial populations. In: 2011 IEEE Symposium on Biological Data Visualization (BioVis), pp. 127–134 (2011)
41. Fuchs, R., Waser, J., Gröller, M.E.: Visual human+machine learning. *IEEE TVCG* 15(6), 1327–1334 (2009)
42. Oeltze, S., Doleisch, H., Hauser, H., Muigg, P., Preim, B.: Interactive visual analysis of perfusion data. *IEEE Transactions on Visualization and Computer Graphics* 13(6), 1392–1399 (2007)
43. Carver, T., Harris, S.R., Berriman, M., Parkhill, J., McQuillan, J.A.: Artemis: An integrated platform for visualization and analysis of high-throughput sequence-based experimental data. *Bioinformatics* 28(4), 464–469 (2012)
44. Franceschini, A., Szklarczyk, D., Frankild, S., Kuhn, M., Simonovic, M., Roth, A., Lin, J., Minguez, P., Bork, P., von Mering, C., et al.: String v9. 1: Protein-protein interaction networks, with increased coverage and integration. *Nucleic Acids Research* 41(D1), D808–D815 (2013)
45. Perer, A., Shneiderman, B.: Integrating statistics and visualization for exploratory power: From long-term case studies to design guidelines. *IEEE Computer Graphics and Applications* 29(3), 39–51 (2009)

46. Kuhn, R.M., Haussler, D., Kent, W.J.: The ucsc genome browser and associated tools. *Briefings in Bioinformatics* 14(2), 144–161 (2013)
47. Thorvaldsdóttir, H., Robinson, J.T., Mesirov, J.P.: Integrative genomics viewer (igv): High-performance genomics data visualization and exploration. *Briefings in Bioinformatics* 14(2), 178–192 (2013)
48. Yang, J., Hubball, D., Ward, M., Rundensteiner, E., Ribarsky, W.: Value and relation display: Interactive visual exploration of large data sets with hundreds of dimensions. *IEEE Transactions on Visualization and Computer Graphics* 13(3), 494–507 (2007)
49. Kehrer, J., Filzmoser, P., Hauser, H.: Brushing moments in interactive visual analysis. *Computer Graphics Forum* 29(3), 813–822 (2010)
50. Meyer, M., Munzner, T., DePace, A., Pfister, H.: Multeesum: A tool for comparative spatial and temporal gene expression data. *IEEE Transactions on Visualization and Computer Graphics* 16(6), 908–917 (2010)
51. Nam, J., Mueller, K.: Tripadvisor-n-d: A tourism-inspired high-dimensional space exploration framework with overview and detail. *IEEE Transactions on Visualization and Computer Graphics* 19(2), 291–305 (2013)
52. Williams, M., Munzner, T.: Steerable, progressive multidimensional scaling. In: *Proceedings of the IEEE Symposium on Information Visualization*, pp. 57–64. IEEE Computer Society, Washington, DC (2004)
53. Endert, A., Han, C., Maiti, D., House, L., North, C.: Observation-level interaction with statistical models for visual analytics. In: *2011 IEEE Conference on Visual Analytics Science and Technology (VAST)*, pp. 121–130. IEEE (2011)
54. Ingram, S., Munzner, T., Irvine, V., Tory, M., Bergner, S., Möller, T.: Dimstiller: Workflows for dimensional analysis and reduction. In: *2010 IEEE Symposium on Visual Analytics Science and Technology (VAST)*, pp. 3–10 (2010)
55. Endert, A., Bradel, L., North, C.: Beyond control panels: Direct manipulation for visual analytics. *IEEE Computer Graphics and Applications* 33(4), 6–13 (2013)
56. Turkay, C., Filzmoser, P., Hauser, H.: Brushing dimensions – a dual visual analysis model for high-dimensional data. *IEEE Transactions on Visualization and Computer Graphics* 17(12), 2591–2599 (2011)
57. Demšar, J., Leban, G., Zupan, B.: Freeviz - an intelligent multivariate visualization approach to explorative analysis of biomedical data. *Journal of Biomedical Informatics* 40(6), 661–671 (2007)
58. Kosara, R., Bendix, F., Hauser, H.: Parallel sets: Interactive exploration and visual analysis of categorical data. *IEEE Transactions on Visualization and Computer Graphics* 12(4), 558–568 (2006)
59. Telea, A., Auber, D.: Code flows: Visualizing structural evolution of source code. *Computer Graphics Forum* 27(3), 831–838 (2008)
60. Lex, A., Streit, M., Schulz, H.J., Partl, C., Schmalstieg, D., Park, P.J., Gehlenborg, N.: StratomeX: Visual analysis of large-scale heterogeneous genomics data for cancer subtype characterization. *Computer Graphics Forum (EuroVis 2012)* 31(3), 1175–1184 (2012)
61. Lex, A., Streit, M., Partl, C., Kashofer, K., Schmalstieg, D.: Comparative analysis of multidimensional, quantitative data. *IEEE Transactions on Visualization and Computer Graphics (Proceedings Visualization / Information Visualization 2010)* 16(6), 1027–1035 (2010)
62. Partl, C., Kalkofen, D., Lex, A., Kashofer, K., Streit, M., Schmalstieg, D.: En-route: Dynamic path extraction from biological pathway maps for in-depth experimental data analysis. In: *2012 IEEE Symposium on Biological Data Visualization (BioVis)*, pp. 107–114. IEEE (2012)

63. Turkay, C., Lex, A., Streit, M., Pfister, H., Hauser, H.: Characterizing cancer subtypes using dual analysis in caleyo stratomex. *IEEE Computer Graphics and Applications* 34(2), 38–47 (2014)
64. May, T., Kohlhammer, J.: Towards closing the analysis gap: Visual generation of decision supporting schemes from raw data. In: *Computer Graphics Forum*, vol. 27, pp. 911–918. Wiley Online Library (2008)
65. May, T., Bannach, A., Davey, J., Ruppert, T., Kohlhammer, J.: Guiding feature subset selection with an interactive visualization. In: *2011 IEEE Conference on Visual Analytics Science and Technology (VAST)*, pp. 111–120. IEEE (2011)
66. Younesy, H., Nielsen, C.B., Möller, T., Alder, O., Cullum, R., Lorincz, M.C., Karimi, M.M., Jones, S.J.: An interactive analysis and exploration tool for epigenomic data. In: *Computer Graphics Forum*, vol. 32, pp. 91–100. Wiley Online Library (2013)
67. Grottel, S., Reina, G., Vrabec, J., Ertl, T.: Visual verification and analysis of cluster detection for molecular dynamics. *IEEE Transactions on Visualization and Computer Graphics* 13(6), 1624–1631 (2007)
68. Dietzsch, J., Gehlenborg, N., Nieselt, K.: Mayday-a microarray data analysis workbench. *Bioinformatics* 22(8), 1010–1012 (2006)
69. Seo, J., Shneiderman, B.: Interactively exploring hierarchical clustering results. *IEEE Computer* 35(7), 80–86 (2002)
70. Guo, Z., Ward, M.O., Rundensteiner, E.A.: Model space visualization for multivariate linear trend discovery. In: *Proc. IEEE Symp. Visual Analytics Science and Technology VAST 2009*, pp. 75–82 (2009)
71. Kandogan, E.: Just-in-time annotation of clusters, outliers, and trends in point-based data visualizations. In: *2012 IEEE Conference on Visual Analytics Science and Technology (VAST)*, pp. 73–82. IEEE (2012)
72. Rinzivillo, S., Pedreschi, D., Nanni, M., Giannotti, F., Andrienko, N., Andrienko, G.: Visually driven analysis of movement data by progressive clustering. *Information Visualization* 7(3), 225–239 (2008)
73. Schreck, T., Bernard, J., Tekusova, T., Kohlhammer, J.: Visual cluster analysis of trajectory data with interactive Kohonen Maps. In: *IEEE Symposium on Visual Analytics Science and Technology, VAST 2008*, pp. 3–10 (2008)
74. Rasmussen, M., Karypis, G.: gCLUTO—An Interactive Clustering, Visualization, and Analysis System., University of Minnesota, Department of Computer Science and Engineering, CSE. Technical report, UMN Technical Report: TR (2004)
75. Ahmed, Z., Weaver, C.: An Adaptive Parameter Space-Filling Algorithm for Highly Interactive Cluster Exploration. In: *Proceedings of IEEE Symposium on Visual Analytics Science and Technology, VAST (2012)*
76. Rubel, O., Weber, G., Huang, M.Y., Bethel, E., Biggin, M., Fowlkes, C., Luengo Hendriks, C., Keranen, S., Eisen, M., Knowles, D., Malik, J., Hagen, H., Hamann, B.: Integrating data clustering and visualization for the analysis of 3D gene expression data. *IEEE/ACM Transactions on Computational Biology and Bioinformatics* 7(1), 64–79 (2010)
77. Turkay, C., Parulek, J., Reuter, N., Hauser, H.: Interactive visual analysis of temporal cluster structures. *Computer Graphics Forum* 30(3), 711–720 (2011)
78. Parulek, J., Turkay, C., Reuter, N., Viola, I.: Visual cavity analysis in molecular simulations. *BMC Bioinformatics* 14(19), 1–15 (2013)
79. Turkay, C., Parulek, J., Reuter, N., Hauser, H.: Integrating cluster formation and cluster evaluation in interactive visual analysis. In: *Proceedings of the 27th Spring Conference on Computer Graphics*, pp. 77–86. ACM (2011)

80. Choo, J., Lee, H., Kihm, J., Park, H.: ivisclassifier: An interactive visual analytics system for classification based on supervised dimension reduction. In: 2010 IEEE Symposium on Visual Analytics Science and Technology (VAST), pp. 27–34. IEEE (2010)
81. Krzywinski, M., Schein, J., Birol, Í., Connors, J., Gascoyne, R., Horsman, D., Jones, S.J., Marra, M.A.: Circos: An information aesthetic for comparative genomics. *Genome Research* 19(9), 1639–1645 (2009)
82. Karr, J.R., Sanghvi, J.C., Macklin, D.N., Gutschow, M.V., Jacobs, J.M., Bolival Jr., B., Assad-Garcia, N., Glass, J.I., Covert, M.W.: A whole-cell computational model predicts phenotype from genotype. *Cell* 150(2), 389–401 (2012)
83. Meyer, M., Munzner, T., Pfister, H.: Mizbee: A multiscale synteny browser. *IEEE Transactions on Visualization and Computer Graphics* 15(6), 897–904 (2009)
84. Piringer, H., Berger, W., Krasser, J.: Hypermoval: Interactive visual validation of regression models for real-time simulation. In: Proceedings of the 12th Eurographics / IEEE - VGTC Conference on Visualization. EuroVis 2010, pp. 983–992. Eurographics Association, Aire-la-Ville (2010)
85. Muhlbacher, T., Piringer, H.: A partition-based framework for building and validating regression models. *IEEE Transactions on Visualization and Computer Graphics* 19(12), 1962–1971 (2013)
86. Booshehrian, M., Möller, T., Peterman, R.M., Munzner, T.: Vismon: Facilitating analysis of trade-offs, uncertainty, and sensitivity in fisheries management decision making. In: *Computer Graphics Forum*, vol. 31, pp. 1235–1244. Wiley Online Library (2012)
87. Meyer, M., Wong, B., Styczynski, M., Munzner, T., Pfister, H.: Pathline: A tool for comparative functional genomics. In: *Computer Graphics Forum*, vol. 29, pp. 1043–1052. Wiley Online Library (2010)
88. Elmqvist, N., Dragicevic, P., Fekete, J.: Rolling the dice: Multidimensional visual exploration using scatterplot matrix navigation. *IEEE Transactions on Visualization and Computer Graphics* 14(6), 1539–1148 (2008)
89. Yang, J., Ward, M.O., Rundensteiner, E.A., Huang, S.: Visual hierarchical dimension reduction for exploration of high dimensional datasets. In: *VISSYM 2003: Proceedings of the Symposium on Data Visualisation 2003*, pp. 19–28 (2003)
90. Berger, W., Piringer, H., Filzmoser, P., Gröller, E.: Uncertainty-aware exploration of continuous parameter spaces using multivariate prediction. *Computer Graphics Forum* 30(3), 911–920 (2011)
91. Malik, A., Maciejewski, R., Elmqvist, N., Jang, Y., Ebert, D.S., Huang, W.: A correlative analysis process in a visual analytics environment. In: 2012 IEEE Conference on Visual Analytics Science and Technology (VAST), pp. 33–42. IEEE (2012)
92. Turkay, C., Lundervold, A., Lundervold, A., Hauser, H.: Representative factor generation for the interactive visual analysis of high-dimensional data. *IEEE Transactions on Visualization and Computer Graphics* 18(12), 2621–2630 (2012)
93. Mirkin, B.: *Core Concepts in Data Analysis: Summarization, Correlation and Visualization*. Springer (2011)
94. Procter, J.B., Thompson, J., Letunic, I., Creevey, C., Jossinet, F., Barton, G.J.: Visualization of multiple alignments, phylogenies and gene family evolution. *Nature Methods* 7, S16–S25 (2010)
95. Otasek, D., Pastrello, C., Holzinger, A., Jurisica, I.: Visual Data Mining: Effective Exploration of the Biological Universe. In: Holzinger, A., Jurisica, I. (eds.) *Knowledge Discovery and Data Mining. LNCS*, vol. 8401, pp. 19–34. Springer, Heidelberg (2014)

96. Mueller, H., Reihs, R., Zatloukal, K., Holzinger, A.: Analysis of biomedical data with multilevel glyphs. *BMC Bioinformatics* 15(suppl. 6), S5 (2014)
97. Tan, P., Steinbach, M., Kumar, V.: *Introduction to data mining*. Pearson Addison Wesley, Boston (2006)
98. van den Elzen, S., van Wijk, J.J.: Baobabview: Interactive construction and analysis of decision trees. In: 2011 IEEE Conference on Visual Analytics Science and Technology (VAST), pp. 151–160. IEEE (2011)
99. Hair, J., Anderson, R.: *Multivariate data analysis*. Prentice Hall (2010)
100. Secrier, M., Schneider, R.: Visualizing time-related data in biology, a review. *Briefings in Bioinformatics*, bbt021 (2013)
101. Chen, C.: Top 10 unsolved information visualization problems. *IEEE Computer Graphics and Applications* 25(4), 12–16 (2005)
102. Jeanquartier, F., Holzinger, A.: On Visual Analytics And Evaluation In Cell Physiology: A Case Study. In: Cuzzocrea, A., Kittl, C., Simos, D.E., Weippl, E., Xu, L. (eds.) *CD-ARES 2013*. LNCS, vol. 8127, pp. 495–502. Springer, Heidelberg (2013)
103. Holzinger, A.: Usability engineering methods for software developers. *Communications of the ACM* 48(1), 71–74 (2005)
104. Kehrer, J., Hauser, H.: Visualization and visual analysis of multifaceted scientific data: A survey. *IEEE Transactions on Visualization and Computer Graphics* 19(3), 495–513 (2013)
105. Matkovic, K., Gracanin, D., Jelovic, M., Hauser, H.: Interactive visual steering-rapid visual prototyping of a common rail injection system. *IEEE Transactions on Visualization and Computer Graphics* 14(6), 1699–1706 (2008)
106. Beale, R.: Supporting serendipity: Using ambient intelligence to augment user exploration for data mining and web browsing. *International Journal of Human-Computer Studies* 65(5), 421–433 (2007)
107. Holzinger, A., Kickmeier-Rust, M., Albert, D.: Dynamic media in computer science education; content complexity and learning performance: Is less more? *Educational Technology & Society* 11(1), 279–290 (2008)
108. Ceglar, A., Roddick, J.F., Calder, P.: Guiding knowledge discovery through interactive data mining. *Managing Data Mining Technologies in Organizations: Techniques and Applications*, 45–87 (2003)
109. Chau, D.H., Myers, B., Faulring, A.: What to do when search fails: finding information by association. In: *Proceeding of the Twenty-Sixth Annual SIGCHI Conference on Human Factors in Computing Systems*, pp. 999–1008. ACM (2008)
110. Olshausen, B.A., Anderson, C.H., Vanessen, D.C.: A neurobiological model of visual-attention and invariant pattern-recognition based on dynamic routing of information. *Journal of Neuroscience* 13(11), 4700–4719 (1993)
111. Chandola, V., Banerjee, A., Kumar, V.: Anomaly detection: A survey. *ACM Computing Surveys (CSUR)* 41(3), 15 (2009)
112. Edelsbrunner, H., Harer, J.L.: *Computational Topology: An Introduction*. American Mathematical Society, Providence (2010)
113. Holzinger, A.: On topological data mining. In: Holzinger, A., Jurisica, I. (eds.) *Knowledge Discovery and Data Mining*. LNCS, vol. 8401, pp. 331–356. Springer, Heidelberg (2014)
114. Bremer, P.T., Pascucci, V., Hamann, B.: Maximizing Adaptivity in Hierarchical Topological Models Using Cancellation Trees, pp. 1–18. Springer (2009)